



Uncertainty arising from sampling

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Introduction

- Does measurement uncertainty include sampling?
- How to estimate uncertainties from sampling
- Uncertainties from sampling in the food sector

Measurement uncertainty



ISO definition

“A parameter, associated with the result of a measurement, that characterises the dispersion of the values that could reasonably be attributed to the measurand”

22.7 ± 4.8 g

The part of the result after the ±

Does measurement uncertainty include sampling?



EURACHEM position

- If the measurand relates to a bulk material from which samples are taken for analysis, the uncertainty in the estimated value for the measurand must include the uncertainty arising from the sampling process
- If the result is reported on the sample ‘as received’ by the laboratory, only within-laboratory sub-sampling contributes to the uncertainty

Examples



- Measuring and reporting the amount of pesticide in a laboratory sample of capsicum (green peppers)
 - Little or no sampling/subsampling
 - Sampling is not part of the measurement process
- Reporting the average level of pesticide in the bulk container (consignment) from which the laboratory sample was taken
 - Sampling may greatly affect the reported result
 - Sampling uncertainty matters

Estimating sampling uncertainty



Different approaches to control of sampling



- Gy: Well respected, based on management and control to eliminate sampling uncertainties
- Sampling uncertainties quantified using replication
 - Ramsey et al
 - Eurachem Guide
- Applying modelling approaches to sampling uncertainty
 - Minkinen et al

Four empirical methods for estimating uncertainty



Method #	Method description	Samplers (People)	Protocols	Component estimated			
				Sampling Precision	Sampling Bias	Anal. Precision	Anal. Bias
1	Duplicates	single	single	Yes	No	Yes	No ¹
2	Multiple protocols	single	multiple	between protocols		Yes	No ¹
3	CTS	multiple	single	between samplers		Yes	Yes ²
4	SPT	multiple	multiple	between protocols +between samplers		Yes	Yes ²

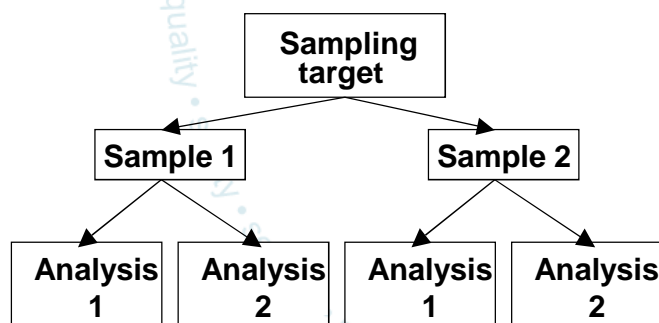
CTS = Collaborative Trial in Sampling, and SPT = Sampling Proficiency Test.

Simplest Empirical method is 'Duplicate Method'

¹ estimate analytical bias using CRM, ² Analytical bias partially or completely included where multiple labs involved

Using the 'duplicate method'

1) Separating sampling and analysis

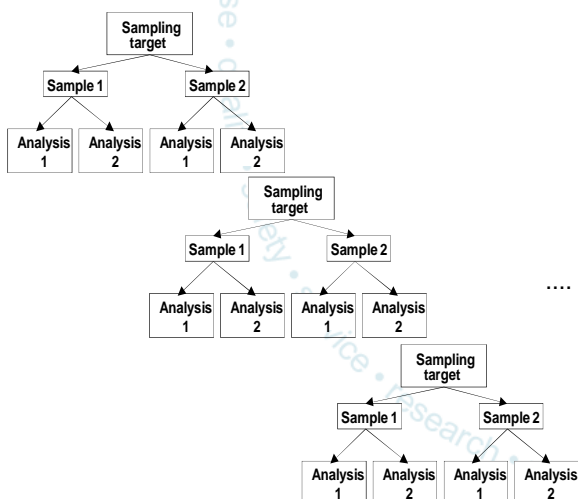


Sampling target:

Portion of material, at a particular time, that the sample is intended to represent.

Using the 'duplicate method'

2) Replicating sampling



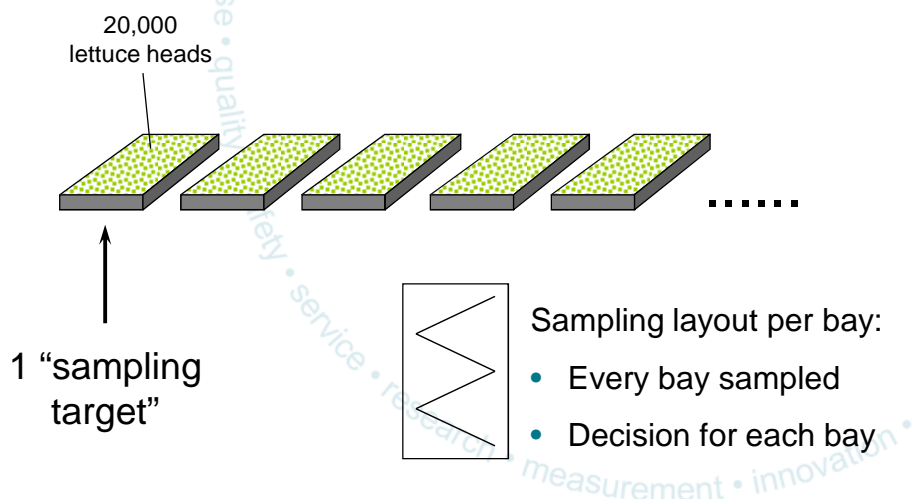
.... to at least 8 sampling targets

Statistical Analysis for the duplicate method


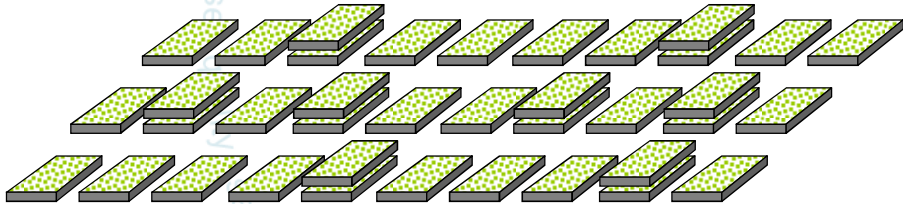


- Fully nested, balanced 2-way layout
- Analysis of variance gives sampling and analytical variance
 - each corresponding to a relevant standard uncertainty contribution
- Robust analysis of variance (RANOVA) suggested for outlier-contaminated data

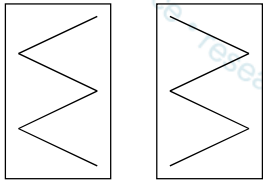
Example: Nitrate in lettuce (Eurachem Guide p 35ff)



Example 1: Duplicate method


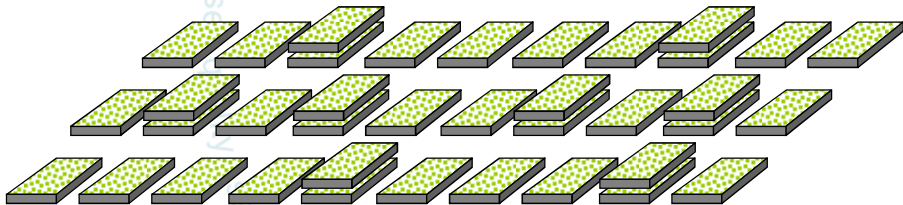



8 (or more) targets sampled in duplicate




Duplicate sampling arrangement

Example: Analysis

Analysis 1

Analysis 2



8 sampling targets

Sampled in duplicate

Each sample duplicate analysed in duplicate

Example: Results



SAMPLE	S1A1	Uncertainty	x - U	x + U	Probabilistic
TARGET					Classification
A	3898	639	3259	4537	Poss Cont
B	3910	641	3269	4551	Poss Cont
C	5708	936	4772	6644	Cont
D	5028	825	4203	5853	Prob Cont
E	4640	761	3879	5401	Prob Cont
F	5182	850	4332	6032	Prob Cont
G	3028	497	2531	3525	Uncont.
H	3966	650	3316	4616	Poss Cont

Example 1: Results




Robust ANOVA:

- $s_{\text{samp}} = 319.05 \text{ mg kg}^{-1}$
- $s_{\text{anal}} = 167.94 \text{ mg kg}^{-1}$
- $s_{\text{meas}} = \sqrt{(s_{\text{samp}}^2 + s_{\text{anal}}^2)} = 360.55 \text{ mg kg}^{-1}$


Classical ANOVA:

- $s_{\text{samp}} = 518.2, s_{\text{anal}} = 148.2; s_{\text{meas}} = 538.9 \text{ mg kg}^{-1}$



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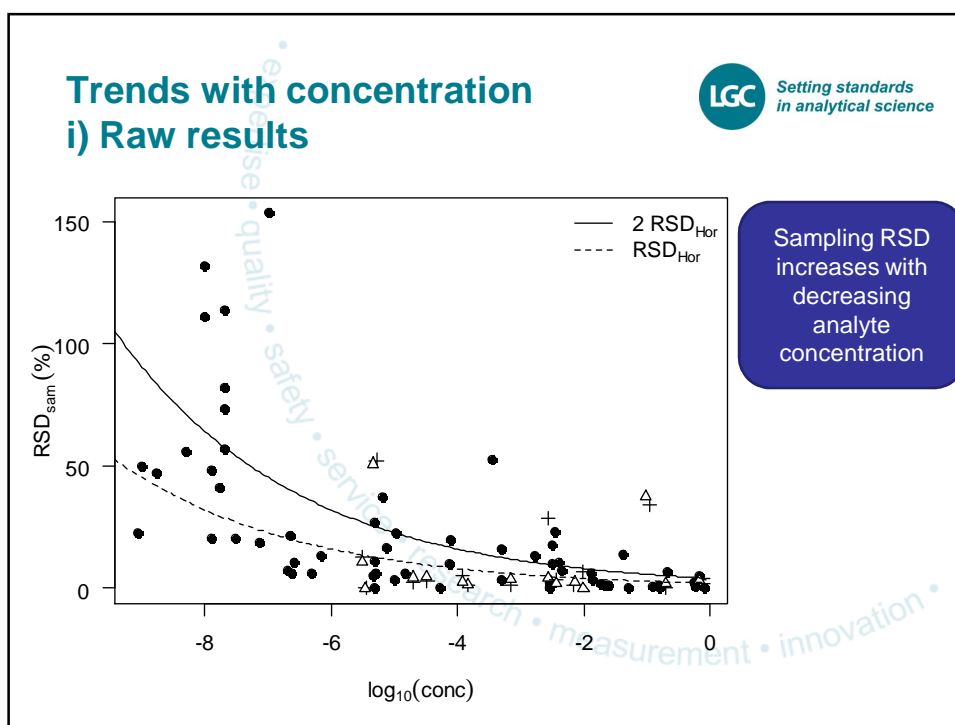
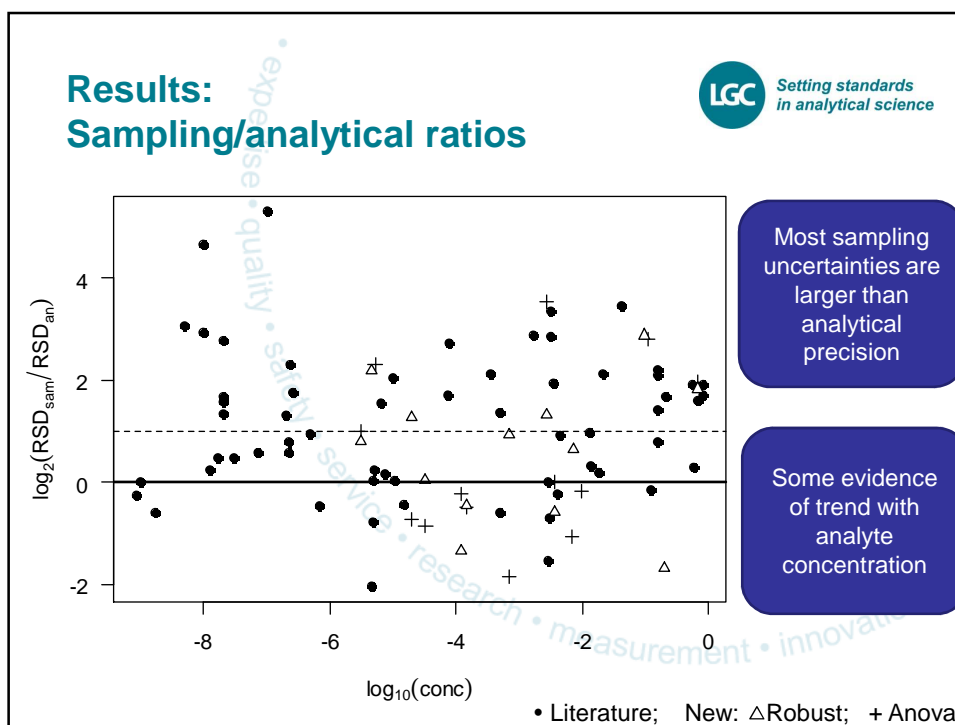
Sampling uncertainties in food analysis



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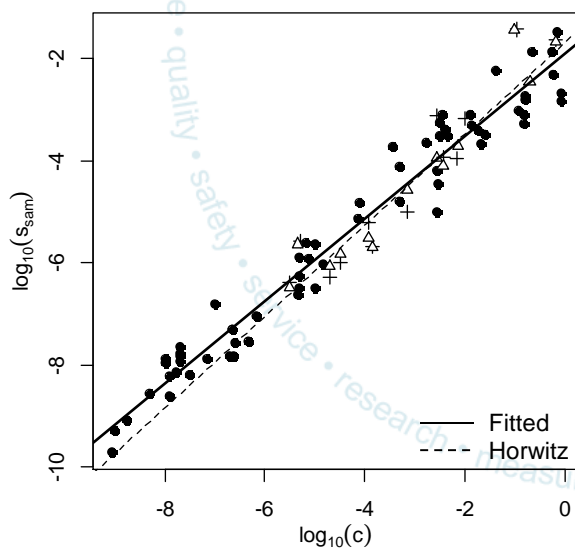
Review of sampling uncertainties in foods: Overview

- Collate available data from literature
 - 23 sources identified
 - 30 product types
 - 59 product/analyte combinations
 - 13 products in retail environments; 17 factory/wholesale
- Apply duplicate method to increase data set on foods of interest
 - A further 16 product/analyte combinations
- Review sampling uncertainties for trends



Trends with concentration

i) log-log relationship



A Horwitz-like function describes sampling SD

The relationship is very approximate

Limitations



- Literature surveys reflect interest in sampling
 - Possibly biased towards known problems
- Experimental work chosen to provide a range of examples
 - not a random sample of sampling
- Values differ from fitted line by about ± 1 in \log_{10} :
 - Approximately one order of magnitude
- Sampling variation need not follow any particular distribution

Practical implementation



- The duplicate method requires a minimum of 8 replicated sampling targets, or 16 sampling exercises
 - Economical only when many more increments are normally taken and measured separately
- Most useful when developing or comparing proposed sampling strategies in practice?

Conclusions



- Primary sampling from the bulk contributes to the uncertainty when the measurand is defined as a property of the bulk material
- Relatively economical empirical approaches to estimating sampling uncertainty are available
- Sampling uncertainties are often considerably larger than analytical uncertainty
- Available data suggest that sampling standard deviation can be predicted to approximately an order of magnitude

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